Feasibility Studies on Guidance and Global Path Planning for Wind-Assisted Montgolfière in Titan

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Abstract—Recent studies have proposed the use of a hot-air (Montgolfière) balloon for possible exploration of Titan, Mars, and Venus. One of NASA’s Outer Planet Flagship mission concepts is the Titan Saturn System Mission, which would be a joint NASA–ESA partnership that plans to employ a Montgolfière along with a lander and an orbiter. This Montgolfière would circle Titan, investigating how Titan and Saturn operate as a system and determining how far prebiotic chemistry has developed. This paper provides a new method to analyze global path planning with balloons on Titan. The main objective of this study is to determine whether the balloon could reach a particular location of interest from a given initial position at its insertion point in the atmosphere using the wind fields on Titan. This study is the first comprehensive analysis and quantitative assessment of balloon guidance in Titan that proactively uses wind for global path planning. The paper will investigate and characterize the guidance and path-planning performance of Montgolfière balloons in Titan’s atmosphere for lower atmosphere and surface exploration in the presence of variable wind fields using the Titan Weather Research and Forecasting (TitanWRF) model. The study focuses on determining the altitude profile that a balloon could follow, using variable wind fields, in order to reach its target most quickly. Our results show that a simple unpropelled Montgolfière without horizontal actuation would be able to reach a broad array of science targets within the constraints of the wind field. The study also indicates that even a small amount of horizontal thrust allows the balloon to reach any area of interest on Titan, in a fraction of the time needed by the unpropelled balloon. The results show that using the Titan wind field allows a balloon to significantly extend its scientific reach and that a Montgolfière (unpropelled or propelled) is a highly desirable architecture that can significantly enhance the scientific return of a future Titan mission.

Index Terms—Decomposition algorithm, general purpose guidance algorithm, global reachability, graph search algorithm, loitering, Markov decision process, Montgolfière, path planning, reachability maps, Titan, TitanWRF.

I. INTRODUCTION

TITAN is ideally suited for aerial vehicle exploration due to its high atmospheric density, its low gravity, and its widely spaced sites of interest. In the case of planets and moons with atmospheres, such as Titan and Venus, a number of authors have proposed the use of aerial systems that can combine extensive coverage with high-resolution data collection and in situ science capabilities. [1]–[4]. Recent studies have proposed the use of a Montgolfière balloon for possible exploration of Titan, Mars, and Venus [2]–[4]. A Montgolfière, which is also known as a hot-air balloon, maintains buoyancy by heating the atmospheric gas inside the balloon. Such a balloon can control its altitude by changing the heating rate or venting gas, but it has no actuation capability in the horizontal plane. The motion of the Montgolfière in the horizontal plane is driven by the local winds. However, it may be possible for the balloon to use the difference in winds at different altitudes to guide itself to a desired location. This approach relies on predictive models of the winds on a planet or moon, such as Titan, which vary both spatially and temporally. These models are known as General Circulation Models, and in recent years, much attention has been devoted to their development, for example [5]–[12]. In our research, we have chosen to make use of the work by Richardson et al. [5], who have developed a general-purpose numerical model of planetary atmospheric and climate dynamics, which is known as PlanetWRF, and its Titan version, which is known as TitanWRF [13]. This general model has been specialized to generate global 3-D wind models for Titan. In planning an aerial mission to Titan, it is extremely important to assess how the moon-wide wind field can be used to extend the navigation capabilities of a balloon, so that widely dispersed science targets can be visited during the mission lifetime, thereby enhancing the scientific return of the mission.

One of the important questions that needs to be addressed is: “What surface locations could the balloon reach from an initial location, and if so how long would it take?” One of the challenging problems in balloon guidance is its limited control authority. In this study, we will develop new path-planning methods for exploration balloons that proactively use the wind field for guidance purposes, combining the knowledge of the wind field with altitude changes and/or horizontal actuation. The primary objective of this study is to demonstrate the advantages of this new approach over passive floating balloons and to answer mission-level questions such as how long it takes to reach potential science targets, how much fuel/energy it consumes, and how much uncertainty the planned path would involve. The resultant product will be a general-purpose guidance algorithm that can be applied to exploration balloons on any moon/planet with an atmosphere, including Titan, Mars, Venus, as well as the gas giants (Jupiter, Saturn, Uranus, and

Neptune). This study will be the first comprehensive analysis and quantitative assessment of balloon guidance that proactively uses wind for global path planning. Unlike existing studies, which are limited to linear wind fields and cannot incorporate more realistic global wind fields with sufficient resolution, our approach will address stochastic, nonlinear, and time-varying wind fields. Through this wind-assisted guidance, we expect to significantly extend the range of the balloon and to reach science targets more quickly, as compared to the simple floater. This approach would also enable repeated visits to a site of interest (“loitering”) that would require significantly less fuel/energy compared to the simple guidance strategy. Results could provide a breakthrough approach for exploration of any planet or moon with a significant atmosphere.

It is important to note that the study did not focus on control strategies for the balloon to track trajectories and was more concerned with finding the optimum trajectory adjustments to take advantage of the wind fields, rather than formulating control algorithms to implement such adjustments in the real system. This work primarily focuses on a high-level guidance architecture with simplified dynamics. A future work can be dedicated to studying the full dynamics of the system and the control strategies that drive the balloon to the desired guidance trajectories in the presence of all kinds of disturbances.

In the analysis, the following options have been explored: a free floater, an unpropelled balloon with altitude control, and a propelled balloon. For a given fixed Titan wind field, or a time-varying TitanWRF wind field representative of northern summer solstice on Titan, we have investigated what regions on the surface of Titan could be reached by the aforementioned balloon options and how much time would be required to reach these regions. Results to date have shown that the regions reachable by an unpropelled Montgolfière depend critically on the latitude/longitude insertion point of the vehicle in Titan’s atmosphere, while a propelled balloon can essentially reach any point on the surface of Titan regardless of the initial insertion state.

The rest of the paper is organized as follows: We first describe Titan and its wind field model briefly. We then present the problem statement and give an overview of Graph Search for Path Planning and Global Reachability. In Section IV, we describe our graph generation approach for deterministic and static (time-invariant) wind fields only. In Section V, we generalize the time-invariant approach to deterministic, but time-varying, wind fields. In Section VI, we describe an approach to solving the path-planning problem in the presence of stochastic uncertainty in the wind field. Finally, Section VII deals with the “loitering” problem, where repeat visits of an interesting site are required.

II. TITAN AND ITS WIND MODEL

Titan is the largest moon of Saturn and the only moon in our solar system to have a substantial atmosphere. The atmosphere is poorly understood and obfuscates the surface, leading to intense speculation about Titan’s nature. The successful entry of the Huygens probe into Titan’s thick nitrogen–methane atmosphere has revealed a new world, which is strangely Earth-like, with methane playing the role of water, low temperature ice substituting for rock, and organic aerosols precipitated from the atmosphere taking the place of soil. Streams of liquid methane flow over the icy bedrock of a world nearly frozen in time shortly after its formation. This complex world is very similar to Earth in many ways. Studying Titan and its prebiotic chemistry can give clues to the origin of life.

TitanWRF is a global model of Titan’s atmosphere, extending from the surface to ~400 km. Based on a global version of the terrestrial Weather Research and Forecasting (WRF) model, TitanWRF basically solves the primitive equations of atmospheric physics (“\(F = ma\)” in a rotating frame plus conservation of mass and energy) discretized onto a 3-D grid. As described in [5] and [13], TitanWRF has been fully adapted to Titan conditions (low gravity, slow rotation rate, atmospheric composition, etc.) and is typically run with ~5° between horizontal grid points and with 55 vertical levels (spaced more closely within Titan’s troposphere, below ~40 km). The model includes parameterizations of turbulent mixing, subsurface heat diffusion, surface energy and momentum exchange, and a radiative transfer scheme for Titan’s thick and hazy N\(_2\)–CH\(_4\) atmosphere. TitanWRF includes the seasonal and diurnal variation in incident solar energy at each location. Finally, TitanWRF includes the gravitational accelerations due to Titan’s eccentric orbit around Saturn. This produces a time-dependent change (“tide”) in the gravitational forcing, which modifies horizontal wind directions and speeds, particularly in the lower atmosphere where background wind speeds are quite low. TitanWRF reproduces many aspects of the real atmosphere, including the observed seasonal and latitudinal variation of surface temperatures and the observed magnitude and seasonal evolution of stratospheric superrotation [13]. We define seasons using Titan’s (Saturn’s) angular position in its orbit around the Sun, i.e., its planetocentric solar longitude \([L_s]\). \(L_s = 0°\) is northern spring equinox, \(L_s = 90°\) northern summer solstice, and so on. Perihelion (the time at which Saturn and thus Titan are closest to the Sun) occurs at \(L_s = 278°\), thus during northern winter/southern summer.

III. PATH-PLANNING APPROACH

In this study, we present a new method for global path planning with Montgolfières that solves both the problems of path planning and reachability [14]. The new method first performs a principled simplification and decoupling of the dynamics of the Montgolfière. This enables us to perform an efficient discretization of the search space, converting the planning problem into a graph search problem. We then use Dijkstra’s algorithm [15] to calculate the minimum-time path from the start location to every possible location in the graph. This solves the reachability problem, and then, for a given desired location, we can extract the minimum-time altitude profile to the goal, thereby solving the path-planning problem. In this study, we show planned paths and reachability maps for a number of scenarios on Titan. The proposed path-planning method is a general-purpose guidance algorithm that can be applied to exploration balloons on any planet or moon with an atmosphere.
We assume that we have a general set of dynamic equations for the Montgolfière in a time-varying wind field of the form

$$\dot{x}(t) = f(x(t), u(t), t)$$

(1)

where $u(t)$ are the heating, venting, and horizontal actuation control inputs applied at time $t$, and $x(t)$ is the state of the Montgolfière at time $t$. Equations in this form are derived in [16], using the thermal and dynamics balloon models in [17]. In this case, the state includes the temperature and volume of the balloon, as well as the 3-D position and velocity of the Montgolfière, which we denote by $r$ and $\dot{r}$, respectively. The dynamics in (1) rely on a predictive model of the winds at any location $r$ and time $t$. We assume that we have such a model in the general form $w(r, t)$. Here, position is defined in a spherical coordinate frame such that

$$r \triangleq \begin{bmatrix} x \\ y \\ z \end{bmatrix}$$

(2)

where $x$ is in degrees longitude, $y$ is in degrees latitude, and $z$ is the altitude from the surface of the planet. Wind velocity is defined in a Cartesian coordinate frame fixed to the local surface tangent such that

$$w(r, t) \triangleq \begin{bmatrix} w_x(r, t) \\ w_y(r, t) \\ w_z(r, t) \end{bmatrix}$$

(3)

where $w_x$, $w_y$, and $w_z$ are the velocities in the eastward, northward, and vertically upward directions, respectively. The coordinate frames are shown in Fig. 1.

The path-planning and reachability problem may now be stated as follows.

**Problem 1:** Given a Montgolfière with dynamics $f(\cdot)$ initially at location $r_0$ and a wind model $w(\cdot)$, determine, for every possible end location $r_f$, the minimum time to reach $r_f$ and the sequence of control inputs $u(\cdot)$ that achieves this minimum.

### A. Related Work

The problem of path planning for Montgolfières was studied in [16] and [18]. In [16], the authors assume that wind fields vary linearly in space and are fixed in time. Given this assumption, they solve the optimal control problem to find the sequence of heating inputs that takes the balloon from its initial state to the goal. The optimal control approach is inherently limited to spatially linear wind fields, whereas the fields predicted by global circulation models may be highly nonlinear. In our previous work, we extended this approach to the case where the wind field consists of a discrete and finite set of layers, each of which has constant wind direction and magnitude [18]. In this case, the wind varies with altitude but not with horizontal location. In this paper, we provide a new method that can handle arbitrary wind fields that vary nonlinearly in the horizontal and vertical directions, as well as in time. Such a capability is necessary given that the available General Circulation Models predict a strong dependence of the winds on all three of these parameters.

A problem that has received considerable attention is that of path planning for autonomous underwater vehicles (AUVs) in current fields [19]–[24]. While the AUVs are assumed to have significant horizontal actuation capabilities, the currents have a significant effect on the motion of the AUV, meaning that this problem shares some aspects of the Montgolfière-path-planning problem. The approach in [24] poses the path-planning problem as a nonlinear optimization problem and uses a “swarm” of feasible paths to provide multiple initial guesses to an optimizer, such as local random search or simulated annealing. The performance of such optimizers is highly dependent on the quality of the initial guess, and in the Montgolfière case, finding feasible paths to use as guesses is very challenging. Alternative approaches use a spatial discretization approach combined with a variety of search techniques to solve the planning problem. Alvarez et al. [19] use a genetic algorithm to search for the optimal path in a 2-D field; however, this search algorithm does not guarantee convergence to a global (or even feasible) solution and does not solve the reachability problem. Garau et al. [20] instead use $A^*$ graph search to guarantee that the optimal path is found; however, this work is restricted to a 2-D time-invariant current field and assumes that the AUV has significant actuation capabilities in the horizontal plane. Petres et al. [21] use a fast-marching search technique to find optimal paths; however, these approaches can return infeasible plans if the current is stronger than the actuation capability of the AUV [23]. This is more often the case with a Montgolfière, which typically has no horizontal actuation capability. Soulignac et al. [23] extend fast-marching techniques to the case where currents are stronger than actuators; however, it is not clear that this extends to the case of a Montgolfière balloon; in addition, Soulignac et al. [23] consider only the path-planning problem and not the reachability problem.

### B. Simplification of Dynamics

The Montgolfière planning problem is complex because it takes place in a 3-D environment. We can, however, simplify the problem using a partial decoupling of the Montgolfière dynamics. This decoupling is based on the following assumptions.

**Assumption 1:** The altitude of the Montgolfière is fully controllable and subject to maximum rise and sink rates, which are denoted by $v_{\text{rise}}$ and $v_{\text{sink}}$, respectively.
Assumption 2: The horizontal velocity of the Montgolfière is proportional to the local horizontal wind velocity at all times.

Assumption 1 comes from the observation that the vertical control authority of the Montgolfière is large compared to the vertical winds predicted by the global circulation models in [5]. This means we can assume that a separate altitude controller exists that issues heating and venting commands to overcome wind disturbances and to drive the Montgolfière to a desired altitude setpoint. This allows us to ignore the effects of vertical winds and the complicated thermodynamic model used in [16] to describe the vertical motion of the Montgolfière.

Assumption 2 comes from Das et al. [16], who use the following relationship for the horizontal dynamics of the Montgolfière:

\[ \dot{r} = \gamma \cdot w(r, t) \]  

where \( \gamma \) is a measure of the drag of the Montgolfière in the horizontal plane. These dynamics mean that, in the horizontal plane, we need to only consider the local wind velocity. We do not need to consider any other thermal or dynamic state of the Montgolfière. This simplification, along with that given by Assumption 1, is critical in efficiently generating a discretized graph, as described in the following sections.

In addition to the model in [16], we assume that the vehicle has horizontal actuators that can generate additional velocity \( u(t) \) with respect to the air. Using Assumption 1 and setting \( \gamma = 1 \), we have

\[ \dot{r}(t) = w(r, t) + u(t) \quad (5) \]

\[ u(t) = [u_x(t) \ u_y(t) \ u_z(t)]^T \quad (6) \]

where

\[ -v_{\text{sink}} \leq u_z(t) \leq v_{\text{rise}} \]

\[ \sqrt{u_x(t)^2 + u_y(t)^2} \leq u_{h, \text{max}} \]

and where \( u_{h, \text{max}} \) is the maximum achievable horizontal actuation.

The key idea to solving a discretized approximation of Problem 1 is to perform an efficient discretization of the search space, converting the planning problem into a graph search problem. We then use Dijkstra’s algorithm to calculate the minimum-time path from the start location to every possible location in the graph.

The graph generation problem may be stated as follows.

Problem 2: Generate a graph \( \mathcal{G} \) consisting of a set of nodes \( S \), where each node \( s_i \in S \) consists of an index \( i \) and a position \( r(s_i) \), a set of arcs between nodes, and a weighted adjacency matrix \( A \) defined such that \( A(i, j) \) is the cost to traverse the arc from \( s_i \) to \( s_j \). \( A(i, j) = \infty \) implies that no arc exists between \( s_i \) and \( s_j \).

Given a graph \( \mathcal{G} \), Dijkstra’s algorithm finds the minimum-cost path from a start node to all other nodes in the graph. The running time of Dijkstra’s algorithm scales with the square of the number of nodes and is hence an appealing algorithm even for large graphs. In this paper, we use Dijkstra’s algorithm to find the minimum-time path between the node nearest to the initial location of the Montgolfière, which is denoted by \( s_i \), and all other nodes. This solves a discretized approximation to the reachability problem. Given the reachability results, the path-planning problem can be simply solved, by extracting the path \( p \in \mathbb{Z}^N \) corresponding to the particular target node \( s_i \). This path consists of a sequence of node indexes, such that \( p(1) = i \) and \( p(N) = l \).

The aforementioned approach was considered for the following cases:

1) deterministic and time-invariant (static) wind fields;
2) deterministic and time-varying wind fields;
3) stochastic and time-varying wind fields.

IV. TIME-INARIANT WIND FIELDS

Here, we consider time-invariant wind fields, such that \( w(r, t) = w(r, T) \) for some fixed \( T \) and all \( t \). In generating the nodes of the graph, we choose to discretize space using a uniform grid, where adjacent nodes are separated by \( \Delta x \) in longitude, \( \Delta y \) in latitude, and \( \Delta z \) in altitude. The decoupling described in Section III-B enables us to consider the discretization of the 3-D search space first in the horizontal plane and then in the vertical plane. We also discretize the horizontal actuation into \( n_h \) vectors that are different in magnitude and/or direction. Thus, each node \( s_i \), known as the source node, corresponds to a particular location \( r \) and an actuation vector \( u(s_i) \).

The weighted adjacency matrix \( A \) is populated as follows. For every node \( s_i \), we use the wind model to determine the local wind \( w(r(s_i), T) \). Considering the horizontal plane first, from (4), the horizontal velocity of the Montgolfière can be written as

\[ \dot{r}(s_i) = w(r(s_i), T) + u(s_i). \]  

We discretize the direction of the Montgolfière velocity in the horizontal plane into one of eight segments, as shown in Fig. 2. Which of these segments the local wind velocity falls into determines the cell that the Montgolfière will transition to if no vertical actuation is applied, which we denote by \( s'_i \). By assuming that the wind is constant in the interval until the next cell is reached, the time taken to travel from \( s_i \) to \( s'_i \) is given by

\[ \Delta t(s_i) = \frac{\text{dist}(r(s_i), r(s'_i))}{\|w(r(s_i), T) + u(s_i)\|}. \]
Fig. 3. Discretization in the vertical plane.

Here, $\text{dist}(\cdot, \cdot)$ is a function that returns the Cartesian distance between two points in a spherical coordinate frame, while $\| \cdot \|$ is the standard vector 2-norm.

By applying vertical actuation, cells above or below $s'_i$ may also be reached (see Fig. 3). In Assumption 1, the vertical range of the Montgolfière depends only on the maximum rise and sink rates and the time available. Hence, the maximum range of the Montgolfière depends only on the maximum rise rate.

The matrix $A$ is therefore given by

$$z_{\text{rise}}(s_i) = \frac{v_{\text{rise}}}{\Delta t(s_i)} z_{\text{sink}}(s_i) = \frac{v_{\text{sink}}}{\Delta t(s_i)}.$$ (11)

The set of cells $\mathcal{R}(s_i)$, for which an arc exists between $s_i$ and $s_j \in \mathcal{R}(s_i)$, is therefore given by

$$s_j \in \mathcal{R}(s_i) \iff \begin{cases} x(s_j) = x(s'_i) \\ y(s_j) = y(s'_i) \\ z(s'_i) - z_{\text{sink}} \leq z(s_j) \leq z(s'_i) + z_{\text{rise}}(s_i). \end{cases}$$ (12)

We can now populate the weighted adjacency matrix $A$. Since Problem 1 requires us to find the minimum time to get from every node to every other node, the cost on an arc must be the time taken to traverse that arc. The matrix $A$ is therefore populated as follows:

$$A(i, j) = \begin{cases} \Delta t(s_i), & s_j \in \mathcal{R}(s_i) \\ \infty, & s_j \notin \mathcal{R}(s_i). \end{cases}$$ (13)

Notice that, although we have discretized space and wind direction, we have retained time and wind magnitude as continuous variables. This ensures that arbitrarily large variations in wind magnitude can be captured without requiring an intractably large number of grid cells. This is essential, since the PlanetWRF wind model predicts winds that vary in magnitude over several orders of magnitude.

In what follows, we define a Titan [solar] day as the time taken for Titan to rotate once (roughly 16 Earth days). Titan is tidally locked, which means that it keeps roughly the same face to Saturn at all times; hence, one Titan day is also the time taken for it to orbit Saturn. Titan is in orbit around Saturn; hence, a Titan year [~673 Titan days] is the same as a Saturn year and lasts roughly 30 Earth years. We also define a Titan hour as 1/24th of a Titan day.

A. Results

Here, we give results demonstrating the graph search algorithm in the time-invariant wind field case. For the following results, winds at time $L_s = 90^\circ$ were used, corresponding to summer solstice with $v_{\text{rise}} = 0.3$ m/s, $v_{\text{sink}} = 0.6$ m/s, and $v_{\text{h, max}} = \{0, 1\}$ m/s.

Fig. 4(a)–(d) shows reachability maps for Titan with no horizontal actuation (only vertical control) at four different starting locations: the north pole, 25$^\circ$ N, the equator, and 45$^\circ$ S. The color in a cell shows how much time it takes for the optimal path from the starting location “S” to all cells across the moon. The color white on the figure shows that the cell is not reachable for that particular starting location. When there is no horizontal actuation, with only the ambient winds and altitude control available to move the balloon, it may take many days to get to a destination of interest, sometimes up to 200 days, and sometimes the location is simply not reachable. Fig. 5(a)–(d) shows global reachability maps for static wind fields with a horizontal actuation of 1 m/s. The color shows number of days that it takes to go from a starting location “S.” As shown in Fig. 5, unlike the case where there is no horizontal actuation, the entire moon is reachable from all four starting locations when there is a horizontal actuation of 1 m/s. It is also interesting to note that, for this actuation level, the time taken to reach a given cell is roughly a factor of 6 shorter.

V. TIME-VARYING WIND FIELDS

This section presents the approach and results with a time-varying wind field. Because the wind at a given location differs depending on when the balloon reaches it, a temporal and spatial discretization is performed. One challenge is that the size of the graph becomes excessive when considering the global reachability problem for planetary exploration. This is because for each dimension (i.e., latitude, longitude, altitude, and time) the size of the graph increases exponentially, and also because of the resolution required to capture the various time scales of the wind field while planning over the long mission duration. In such cases, the memory requirement for graph construction and the search algorithm becomes fairly significant.

To address this issue, a decomposition algorithm for a reachability analysis of a time-varying graph has been developed. Because the balloon only moves in the positive direction in time, the adjacency matrix of the graph can be represented with an upper block-triangular matrix, and this upper block-triangular structure can be exploited to decompose a graph search problem. Instead of solving a single large problem, our algorithm solves subproblems sequentially whose size is far smaller than the original problem. The new approach therefore consumes much smaller amounts of memory, which also helps speed up the overall computation when the computing resource has a limited physical memory compared to the problem size.

A. Problem Statement—Decomposition Algorithm

Let $n_s$ denote the number of starting nodes. Each node $s_i$ is a function of the position $(x_i, y_i, z_i)$ and time $t_i$. A uniform grid is used to represent the world, and we let $n_x, n_y, n_z,$ and $n_t$ respectively denote the number of cells in the $x$-, $y$-, $z$-, and time-axes. We define $n_r = n_x n_y n_z$ as the number of cell positions in the environment and $N = n_t n_r$ as the total
number of cells. The problem statement for the graph search is to find the shortest paths from \( n_s \) starting nodes \( s_i \) to all \( n_r \) 3-D locations. Once the graph is constructed, it is straightforward to apply Dijkstra’s algorithm to find the shortest paths. A matrix of size \( n_s \times n_r \) can represent the minimum time of arrival at each 3-D location from each starting node. Let this matrix be denoted by \( C^* \). Its \((p, q)\) element \( C^*_{pq} \) stores the time of travel from the \( p \)th starting location to the \( q \)th 3-D location and is set to be \( \infty \) if there exists no such trajectory.

The primary components of the time-varying wind field of Titan include 1) seasonal changes in the global atmospheric circulation driven by the changing solar forcing as Saturn orbits the Sun (period of one Titan year, \( \sim30 \) Earth years), 2) tidal effects driven by Titan’s eccentric orbit around Saturn (period of one Titan day, \( \sim16 \) Earth days), and 3) small- and large-scale waves occurring naturally in Titan’s atmosphere on a range of time-scales. A potential future mission to explore Titan would have a mission duration of 6–12 Earth months, and capturing the time-varying wind field of various time scales would require a large \( n_t \) to be used in the graph.

Fig. 6 shows the adjacency matrix of the graph, which is of size \( N \times N \). Because the balloon only moves in the positive direction in time, it can be represented with an upper block-triangular matrix, by ordering the nodes in terms of their time \( t_i \). Each block contains a snapshot of the 3-D world, whose size is \( n_r \times n_r \). With a large \( n_t \), the memory requirement for graph construction and Dijkstra’s algorithm becomes significant. However, this upper block-triangular structure of the adjacency matrix can be exploited to decompose the problem into several smaller subproblems that use far less memory.
We assume the balloon starts at $t = 0$, so that all the starting nodes are in the $(1, 1)$ block. This approach splits the weighted adjacency matrix $A$ into several submatrices $M_k$, $k = 1, \ldots, k_{\text{max}}$ and repeatedly applies Dijkstra’s algorithm to each submatrix. The result of each subproblem can be represented by a matrix, whose size is much smaller than the submatrix used in the subproblem. The next subproblem is formed, by appending to its submatrix the small matrix obtained in the previous subproblem. This process is repeated until all the submatrices are processed or all the shortest paths from the starting nodes to the 3-D locations are found. A detailed discussion of the algorithm is available in [25].

### B. Simulation Results

Fig. 7 shows several trajectories from a start location of $(5^\circ$ S, $5^\circ$ E) to three different goals $G_1$ ($5^\circ$ S, $155^\circ$ E), $G_2$ ($75^\circ$ S, $85^\circ$ W), and $G_3$ ($85^\circ$ N, $85^\circ$ E). The size of the circles...
represents the elapsed time from start, and the color of the circles represents the altitude of the trajectory. Note that, because of the nonlinear and time-varying wind field, the minimum-time trajectories involve several vertical actuation steps and are far from straight lines.

Fig. 8 shows the percentage of the areas of Titan’s surface that would be reachable in a given time with four different horizontal actuation levels (0.0 m/s, 0.25 m/s, 0.50 m/s, and 1.0 m/s). For example, 50% on the y-axis means that 50% of the points on Titan’s surface could be reached in a given time if set as a destination; it does not mean that the balloon would sweep over 50% of the Titan surface in this time. The plots have 24 different starting locations with the following combinations of longitude and latitude:

1) four longitudes (175° W, 85° W, 5° E, 95° E);
2) six latitudes (85° S, 45° S, 15° S, 15° N, 45° N, 85° N).

Because the wind field varies far more with latitude than with longitude, the lines corresponding to the same latitude are plotted with the same color and show similar trends: for example, a balloon starting at 15° S (shown in red) can initially reach only limited areas, but the reachable area grows rapidly after a few months, whereas for a balloon starting near the southern pole at 85° S (shown in blue), the reachable area does not grow as fast with time.

It is clear that both the reachable area and the time of arrival dramatically improve, by allowing more horizontal actuation. In addition, note that, with no horizontal actuation (i.e., 0.0 m/s), some of the area is not reachable, in the time shown.

VI. UNCERTAIN WIND FIELDS

In practical applications, the wind vector field is not known exactly and may deviate significantly from the wind velocities estimated by the TitanWRF model. This section describes how the problem framework may also be adapted for uncertain wind fields for probabilistic solution methods. Our primary contribution in this scenario is in appropriately formulating the problem as a Markov decision process (MDP), for which a number of solution methods may be applied.

A. Approach

With uncertain wind fields, the transition from each state is no longer deterministically specified by the wind model as it was in the graph solution aforementioned. From a given state $s_i$, the next state, which is dubbed $s'_i$, may be considered a random variable, and the corresponding probability distribution for $s'_i$ can be constructed over all horizontally adjacent cells. Given these transition probabilities from all states, we wish to select the actions (horizontal and vertical actuation of the Montgolfière) that minimize time-to-goal. This optimality problem is thus naturally posed as an MDP ($S, A, P, R$), where $S$ represents the set of possible states, i.e., $(x, y, z)$ locations, of the Montgolfière; these are the same discretized longitude/latitude/altitude cell positions, as defined for the graph $G$ in Section IV. $A$ is the set of actions available from each state, namely, the combination of horizontal and vertical actuation options. $P$ gives the transition probabilities between states under a given action: given current state $s_i$ and action $a$, $P_a(s_i, s_j) = Pr[s'_j = s_j | s_i, a]$. $R$ defines the expected immediate reward for each transition and each action $a$. Since we wish to optimize for the least travel time, we use a reward of negative travel time (or, equivalently, a cost of positive travel time).

In order to model the wind uncertainty, we choose to decompose it into direction and magnitude components and assign independent distributions, each with an expected value equal to the field model value. Let $\bar{w}(r_i, t)$ denote the (random) wind velocity at position $r_i$ at time $t$ and $\bar{w}(r_i, t)$ denote the velocity given by the wind field (TitanWRF) model. The direction and magnitude of $\bar{w}(r_i, t)$ are represented by $\theta_i$ and $w_i$, respectively. The wind direction $\theta_i$ is of primary importance as it principally determines the next horizontal cell of the vehicle. To model the uncertainty in $\theta_i$, we employ the von Mises distribution, i.e., an analog of the Gaussian distribution on the circle. The von Mises distribution is defined by

$$f_{VM}(\theta_i | \phi_i, \kappa) = \frac{\exp(\kappa \cos(\theta_i - \phi_i))}{2\pi I_0(\kappa)}$$

where $\phi_i$ is the mean, $\kappa$ is a concentration parameter, and $I_0(\kappa)$ is the modified Bessel function of the first kind of order 0. We set $\phi_i$ to the angle given by the wind field model at position $r_i$, i.e., $\phi_i = \angle(\bar{w}(r_i, t))$, and $\kappa$ to a constant chosen by the user. Note that $\kappa$ could be also chosen to vary by position if desired.

The wind magnitude $w_i$ uncertainty is modeled as Gaussian, with distribution

$$f_N(w_i | \mu_i, \sigma_i^2) = \frac{1}{\sqrt{2\pi\sigma_i^2}} \exp\left(-\frac{(w_i - \mu_i)^2}{2\sigma_i^2}\right).$$

Here, we set the mean to the value given by the wind field model, i.e., $\mu_i = |\bar{w}(r_i, t)|$, and the standard deviation set as proportional to the magnitude, i.e., $\sigma_i = \rho |\bar{w}(r_i, t)|$. The value of $\rho$ is chosen by the user. Next, we define the transition probabilities $P_a(s_i, s'_i)$ that govern what state $s'_i$ is entered after executing each action $a$ from each state $s_i$. Note that all uncertainty is limited to the horizontal direction; the vehicle will transition to a selected altitude with probability 1, provided that the action is allowable (i.e., that the altitude is reachable based on vertical actuation limits). Thus, for the following discussion, only the projections onto the horizontal plane are relevant.
Let us first address the situation where there is no horizontal vehicle actuation. In this case, the wind direction wholly determines the next state’s horizontal position, and the action space consists only of the selection of the next altitude from those possible under the constraints of $v_{\text{rise}}$ and $v_{\text{sink}}$. Hence, for each horizontal slice within the allowable altitudes dictated by $a$, the probability of the wind forcing the Montgolfière from state $s_i$ to a horizontally adjacent state $s_j$ is

$$P_a(s_i, s_j) = \frac{\theta_{ij} + \frac{\pi}{4}}{\int_{\theta_{ij}}^{\theta_{ij} + \frac{\pi}{4}} f_{VM}(\theta|\phi_i, \kappa) \, d\theta} \text{ (16)}$$

where $\theta_{ij}$ is the smaller bordering angle of the one-eighth circular sector pointing from $s_i$ to $s_j$. Note that this integration must be accomplished numerically, as no closed-form solution exists.

Next, let us address the use of horizontal vehicle actuation. As before, horizontal actuation is accounted for via an additive velocity on top of the wind velocity. In the stochastic case, we still treat the actuation as known, but the direction and magnitude of the wind are now uncertain. We are interested in the transition governed by the resultant velocity, i.e., $\mathbf{v}_{i,a} = \mathbf{w}(r_i, t) + \mathbf{u}_a$.

A Monte Carlo method is used to determine the probabilities $P$ of and expected rewards $R$ from the resultant vector for each action, as follows. First, a set $\Theta_0$ of $N$ sample points and a set $W_0$ of $N$ samples are drawn from the von Mises distribution $f_{VM}(\theta|0, \kappa)$ and the standard normal distribution, respectively. (This step is required only once, whereas the following steps must be done by iterating for each state $s_i$.) Second, we adjust these samples for state $s_i$. The wind direction samples are rotated by $\phi_i$, i.e., $\Theta_i = \Theta_0 + \phi_i$, and the wind magnitude samples are adjusted by $W_i = \sigma_i W_0 + \mu_i$ (pardonning the abuse of notation, each sample in $\Theta_0$ and $W_0$ is adjusted individually). Third, we calculate the resultant velocity samples, by converting the random wind samples to Cartesian coordinates and adding the horizontal actuation

$$\mathbf{v}_{i,a} = \mathbf{W}_i \begin{bmatrix} \cos \Theta_i \\ \sin \Theta_i \end{bmatrix} + \mathbf{u}_a \text{ (17)}$$

where again the operations involving $W_i$ and $\Theta_i$ are performed element-wise.

Once we have the resultant samples $\mathbf{V}_{i,a} = \{\mathbf{v}_{i,a}^n\}_{n=1}^N$, we can calculate the transition probabilities $P_i$, which are simply made by counting the samples in each circular sector corresponding to $s_j$, i.e.,

$$P_a(s_i, s_j) = \frac{1}{N} |V_{ij,a}| \text{ (18)}$$

where $|\cdot|$ represents cardinality and

$$V_{ij,a} = \left\{ \mathbf{v}_{i,a}^n \mid \angle \mathbf{v}_{i,a}^n \in \left[ \theta_{ij}, \theta_{ij} + \frac{\pi}{4} \right] \right\} \text{ (19)}$$
B. Action Space and Rewards

Minimum travel time is the goal of our MDP solution, and thus, travel time is still appropriate to use as a transition cost. Note that we do not know the resultant velocity exactly but that we seek the expected reward for the MDP. We estimate the expected value of the velocity magnitude as the population mean of the aforementioned Monte Carlo samples, i.e.,

$$\langle v_{i,a} \rangle = \frac{1}{N} \sum_{n=1}^{N} \|v_{i,a}^n\|.$$  (20)

The expected immediate reward for the transition from $s_i$ to $s_j$ under action $a$ is then

$$R_a(s_i, s_j) = -\frac{d_{ij}}{\langle v_{i,a} \rangle}.$$  (21)

where $d_{ij} = \sqrt{(x_j - x_i)^2 + (y_j - y_i)^2}$ is the horizontal distance from $r_i$ to $r_j$. Note that the reward is negative to enforce elapsed time as a “cost.” Note also that the travel time is identical for all actions $a$ that have the same horizontal actuation (i.e., travel time is not dependent on altitude choice).

C. Solving for Minimum Time-to-Goal

To complete the problem setup, we define a goal location for the Montgolfière and create a sink state at this location. All transitions leaving the sink state $s_g$ have zero probability; it is the only state where the vehicle can remain stationary (or, more precisely, once in $s_g$, the vehicle returns to $s_g$ with probability 1 and zero reward). Thus, the cumulative reward will decrease with every transition until the vehicle reaches the goal location $s_g$.

Given this setup, the MDP solution will determine, for each given current state $s_i$, what is the optimal immediate action $a \in A_i$, so that the expected cumulative time-to-goal is minimal. This collection of actions is referred to as the optimal policy $\pi^*$. Note that this differs conceptually from the deterministic graph search method, which instead defines the initial state and determines the cost to reach each other cell from this location.

An undiscounted ($\gamma = 0$) MDP solution method is appropriate because we are interested in the cumulative time elapsed from start to goal. Then, the total expected reward of a state $s_i$ (value of $s_i$ under policy $\pi^*$) $V^*(s_i)$ indicates the expected value of the travel time from a given state $s_i$ to the goal state. The value $V^*(s_i)$ thus provides the information needed in our “reachability” plots, which, for the MDP case, now represent the expected time-to-goal (rather than time-from-start as in the deterministic case).

D. Results

We applied the aforementioned approach for planning paths in uncertain wind fields to simulations of a Montgolfière balloon in the atmosphere of Titan. Nominal wind field values were again taken from the TitanWRF model [5]. The MDP was solved via value iteration until the maximum change in value over all states changes less than $\epsilon = 1$ [Earth day] between iterations.

Fig. 9 displays the expected time-to-goal (AKA time-to-go) of the vehicle from anywhere on the Titan globe. The expected time-to-goal is equivalent to the “value” $V(s_i)$ of the state. For each plot, only one horizontal slice (at $z = 1000$ m) is shown. Note that these figures are different from the “reachability” plots in the previous section, which plot the time to reach the
cell from a given start position; here, we are given the goal location and show how long we expect to take to reach it. In addition, the time is an expected value, since the actual time is uncertain. The path is randomly generated from a manually selected starting location (20\(^\circ\) N, 0\(^\circ\) E), following an optimal policy, and moving according to the state transition probabilities \(P\). The size of the circle along the path increases with time to show the progress of the vehicle, while the color inside the circle indicates vehicle altitude. Note that, since the transitions are uncertain, visiting the same location multiple times may result in different transitions, as happens in the unactuated case.

It is clear that the use of actuation greatly aids the vehicle in reaching the goal. (Note that the color bars are plotted on different scales; hence, the colors cannot be compared directly.) Particularly in the case of the goal nearest to the southern pole, the goal cannot be reached (in the time shown) from several locations without the aid of actuation. A more detailed description of algorithms is discussed in [26].

VII. LOITERING

The methods described in the preceding sections enable path planning for a Montgolfière to reach the location of a desired science target, either through vertical actuation alone or combined with limited horizontal actuation. Once arrived at the target, however, the limitation or lack of horizontal actuation presents a new problem:

1) Given that the vehicle has reached its target location cell, how long can it remain in that cell to perform science observations?

One obvious solution—dropping an anchor—may not be practical for the Titan mission due to altitude and mass considerations. Instead, we consider again using the wind field predictions. If the altitude is not constrained, then we can position the Montgolfière at the altitude of smallest horizontal wind magnitude to maximize the time spent within the target cell. Eventually, the Montgolfière may drift out of the science target cell. If the mission requires further observations of the target cell, it would be useful to determine if the Montgolfière could repeatedly return to the same cell given the predicted wind fields, i.e., find the shortest time or distance cycle path that includes the science target cell. Our reachability graphs can be used both to calculate hover times and to plan the shortest possible path to return to the target.

A. Minimum Wind Speeds and Maximum Hover Times

Wind speed extrema were determined, by linearly interpolating the horizontal wind velocity components to 50-m intervals in altitude for each latitude and longitude grid point, computing the vector magnitude, and sorting by magnitude within each vertical column of cells. Fig. 10 illustrates the predicted minimum speeds for a stationary Titan wind field (at time \(L_s = 0\)), at the model’s highest spatial resolution (5\(^\circ\) × 5\(^\circ\) × 500 m). The minimum horizontal speeds range from near zero to over 2 m/s. At this time of year, minimum wind speeds in the southern hemisphere are generally lower than in the northern hemisphere and range up to around 1 m/s. For comparison purposes, the maximum wind speeds for the same point in time, as shown in Fig. 11, range to over 5 m/s.

To help illustrate the benefit of adding horizontal actuation, Fig. 12 shows a coarser contoured version of the minimum speed data in Fig. 10, binned to 0.25-m/s intervals. In Table I, the area of each colored contour was summed cumulatively and divided by the total area, to estimate the fraction of cells at each actuation level in which the vehicle can hover indefinitely. For example, with an onboard actuation capability of 0.5 m/s, the vehicle would be able to hover indefinitely over greater than half of the total number of surface locations.

Without horizontal actuation, the smallest horizontal wind speed is usually found at the altitude corresponding to the
longest duration adjacency arc in $A(i, j)$. However, $A(i, j)$ also depends on cell shape and size; hence, it is a better indicator than the wind speed of the actual loitering time within a given cell. Using max $A(i, j)$ at each latitude and longitude, the predicted maximum hover times for the stationary wind field are shown in Fig. 13, for the case of no horizontal actuation. Calculating the maximum hover time is straightforward to extend to the nonstationary or stochastic wind field models: substitute the new search methods and weighted adjacency matrices, as defined in the preceding chapters.

### B. Minimum Closed Cycle in a Stationary Wind Field

After the Montgolfière drifts out of a science target cell, we can use our graph search tools to find the shortest time or distance cycle path to return to the target cell. For the general case of locating cycles in a directed graph, there are reported methods available.

However, for our case, we know the initial science target cell and can take advantage of our precomputed weighted adjacency matrix, which means that a more straightforward approach is feasible. Given a desired science target cell $s_i$ and a weighted adjacency matrix $A(i, j)$ for a wind field grid, the minimum-time closed cycle to return to cell $s_i$ after drifting out can be determined as follows:

1. Determine $R(s_i)$, the set of all cells $s_j$ adjacent to $s_i$, using the methods outlined in Section IV on Graph Construction.
2. For each reachable cell $s_j$ in $R(s_i)$, run the shortest path algorithm in Section IV from $s_j$ with $s_i$ as the end goal.

If the science target requires us to be at a particular altitude, then we must also perform path searches for all of the $L$ possible starting altitudes. Due to the overlap of the adjacent nodes, in the worst case, we have to perform only $8L$ path searches. In practice, the computation is more tractable because not all eight directions will be reachable from the science target location, and the set of adjacent cells for a given starting altitude will often overlap with adjacent cells of other starting altitudes.

We can increase the graph search efficiency, by reducing the graph size with distance or time constraints. Assuming the Montgolfière must return to $s_i$ within a desired time $T_d$, or travel no farther from $s_i$ than distance $D$, then we can first determine the reachability map from $s_i$ as the starting point and remove all cells from the graph that are farther than $T_d$ in time, or $D$ in distance, before searching the remaining graph for the shortest possible cycles.

### VIII. Conclusion

In this paper, we have presented a new path-planning approach for local and global path planning of propelled and unpropelled hot-air (Montgolfière-type) balloons operating in Titan’s atmosphere. This planning approach enables a Montgolfière to exploit variations in the wind field at different altitudes to achieve a desired horizontal motion. The approach was extended to the time-varying wind fields, which significantly increased the computational complexity. A new decomposition method has been developed that requires less memory and computation time compared to the original approach. To account for the uncertainties in the wind fields, a stochastic formulation was also presented. It was shown that, by using a spatial and temporal discretization combined with existing graph search techniques, we can determine the altitude profiles that reach a target in minimum time, determine the set of all reachable targets from a given start location, and provide a reachability analysis for the entire moon. This new approach was applied to different scenarios, and the performance of a free floater, an unpropelled balloon with altitude control, and a propelled balloon was examined. It was shown that, given a small amount of horizontal actuation, the balloon will be capable of reaching more targets on Titan, given a limited mission duration, and of reaching all targets more quickly than a passive balloon. Moreover, in the cases where there is a need to repeatedly visit (or “loiter” over) a science target, it was shown that the cycle times dramatically decrease when an actuated balloon is used. Therefore, use of actuation clearly helps the vehicle to reach its target faster and to remain there if desired.

Primarily, the focus of this paper has been on trade studies and quantitative assessments of balloon guidance performance on Titan based on approximate dynamics of the balloon. These guidance trajectories are as valid as the wind field models, and using a finer grid for the wind fields, one can generate finer guidance trajectories. It is important to note that the study did not focus on the control problem for the balloon to track these trajectories and more work is required to study it. A future work can be dedicated on studying the full dynamics of the system and control strategies that could drive the balloon to the desired guidance trajectories in the presence of all kinds of realistic disturbances.
The proposed path-planning method provides a quantitative assessment of guidance performance, science return assessment, and sensitivity of mission performance to key parameters, which will have significant impact on design choices and trade studies for cost-effective future balloon missions. The reachability analysis is critical in performing trade studies to determine the right aerial system to use and where and when such a system should be deployed for maximum science return. This path-planning tool is a general-purpose guidance algorithm that can be applied to exploration balloons on any moon/planet with atmosphere, including Titan, Mars, Venus, and the gas giants, provided that wind field models are available.

REFERENCES


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